

Multiple-choice exam:	GRA 60352	Mathematics		
Examination date:	19.04.2013	09:00 - 10:00	Total no. of pages:	5 incl. attachments
			No. of attachments:	1 (1 page)
Permitted examination	A bilingual dictionary and BI-approved calculator TEXAS			
support material:	INSTRUMENTS BA II Plus			
Answer sheets:	Answer sheet for multiple-choice examinations			
	Counts 20%	of GRA 6035	The questions have e	equal weight
Re-take exam			Responsible departm	ent: Economics

#### PLEASE READ THE FOLLOWING BEFORE YOU BEGIN!

- Students must themselves assure that the examination papers are complete.
- Students must provide the following information on the answer sheet:
  - Examination code
  - Personal initials
  - ID-nr

The ID-nr must be recorded with both the appropriate numbers and by putting an "X" by the corresponding number in the columns below.

- Do not use pencils or pens with green ink when filling in answer sheets. Answer sheets must not be used for rough drafts.
- All answers must be recorded with an "X" under the letter you believe corresponds with the correct answer.
- Cancel an "X" by filling in the box completely (boxes that are completely filled in will not be registered). "X" in two boxes for one question will be registered as a wrong answer.
- The attached example shows you how the answer sheet would be filled in if A were the correct answer for question 1, B correct for question 2, C correct for question 3 and D correct for question 4. An "X" under E indicates that you choose not to answer question 5.
- Your answers are to be recorded on the answer sheet. Answers written on the examination papers and not on the answer sheets will not be graded.
- There is only <u>one</u> right answer for each question. Because the questions are weighted equally, it can be to your advantage to answer the easiest questions first.
- Wrong answers are given -1 point, unanswered questions get 0 points (indicated by an "X" next to E") and correct answers are given 3 points.
- You can keep the examination papers.

# This exam has 8 questions

QUESTION 1.

Consider the linear system with augmented matrix

$$\begin{pmatrix}
0 & 2 & -3 & 1 & 4 \\
-2 & 8 & -5 & -5 & -2 \\
1 & -1 & -2 & 4 & 7
\end{pmatrix}$$

#### Which statement is true?

- (a) The linear system is inconsistent.
- (b) The linear system has one degree of freedom
- (c) The linear system has two degrees of freedom
- (d) The linear system has three degrees of freedom
- (e) I prefer not to answer.

# QUESTION 2.

Consider the vectors  $\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$ , given by

$$\mathbf{v}_1 = \begin{pmatrix} 0 \\ 2 \\ -3 \\ 1 \end{pmatrix}, \quad \mathbf{v}_2 = \begin{pmatrix} -2 \\ 8 \\ -5 \\ -5 \end{pmatrix}, \quad \mathbf{v}_3 = \begin{pmatrix} 1 \\ -1 \\ -2 \\ 4 \end{pmatrix}$$

### Which statement is true?

- (a) The vectors  $\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$  are linearly independent
- (b) The vectors  $\{\mathbf{v}_1, \mathbf{v}_2\}$  are linearly independent, and  $\mathbf{v}_3$  is a linear combination of  $\{\mathbf{v}_1, \mathbf{v}_2\}$
- (c) The vectors  $\{\mathbf{v}_1, \mathbf{v}_2\}$  are linearly independent, but  $\mathbf{v}_3$  is not a linear combination of  $\{\mathbf{v}_1, \mathbf{v}_2\}$
- (d) The vectors  $\{\mathbf{v}_1, \mathbf{v}_2\}$  are not linearly independent
- (e) I prefer not to answer.

### QUESTION 3.

Compute the rank of the matrix

$$A = \begin{pmatrix} 0 & 2 & -3 & h & 4 \\ -2 & 8 & -5 & -5 & -2 \\ 1 & -1 & -2 & 4 & 7 \end{pmatrix}$$

#### Which statement is true?

- (a)  $\operatorname{rk} A = 2$  for all h
- (b)  $\operatorname{rk} A = 3$  for  $h \neq 1$  and  $\operatorname{rk} A = 2$  for h = 1
- (c)  $\operatorname{rk} A = 3$  for  $h \neq 1$  and  $\operatorname{rk} A = 1$  for h = 1
- (d)  $\operatorname{rk} A = 2$  for  $h \neq 1$  and  $\operatorname{rk} A = 1$  for h = 1
- (e) I prefer not to answer.

# QUESTION 4.

Consider the matrix

$$A = \begin{pmatrix} -1 & 3 \\ 4 & 0 \end{pmatrix}$$

### Which statement is true?

- (a) A has eigenvalues  $\lambda = 3$  and  $\lambda = -4$
- (b) A has eigenvalues  $\lambda = -1$  and  $\lambda = 0$
- (c) A has a single eigenvalue  $\lambda = 3$
- (d) A has eigenvalues  $\lambda = 3$  and  $\lambda = 4$
- (e) I prefer not to answer.

### QUESTION 5.

Consider the matrix A and the vectors  $\mathbf{u}, \mathbf{v}$  given by

$$A = \begin{pmatrix} -1 & 3 \\ 4 & 0 \end{pmatrix}, \quad \mathbf{u} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}, \quad \mathbf{v} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

#### Which statement is true?

- (a) Both  $\mathbf{u}$  and  $\mathbf{v}$  are eigenvectors of A
- (b) Neither  $\mathbf{u}$  nor  $\mathbf{v}$  are eigenvectors of A
- (c) The vector  $\mathbf{u}$  is an eigenvector of A, but  $\mathbf{v}$  is not
- (d) The vector  $\mathbf{v}$  is an eigenvector of A, but  $\mathbf{u}$  is not
- (e) I prefer not to answer.

#### QUESTION 6.

Consider the quadratic form

$$Q(x_1, x_2) = hx_1^2 - 4x_1x_2 + 3x_2^2$$

### Which statement is true?

- (a) Q is positive semidefinite for all h
- (b) Q is positive semidefinite when  $h \geq 0$ , and indefinite otherwise
- (c) Q is positive semidefinite when  $h \geq 0$ , and negative semidefinite otherwise
- (d) Q is positive semidefinite when  $h \geq 4/3$ , and indefinite otherwise
- (e) I prefer not to answer.

### QUESTION 7.

Consider the function f given by

$$f(x,y) = x^4 + x^2 - 2xy + hy^2$$

# Which statement is true?

- (a) f is a convex function for all h
- (b) f is a convex function for  $h \geq 0$ , and concave otherwise
- (c) f is a convex function for  $h \geq 1$ , and neither convex nor concave otherwise
- (d) f is a convex function for  $h \ge 1$ , and concave otherwise
- (e) I prefer not to answer.

# QUESTION 8.

The function f(x,y,z)=x+2y+4z is defined on the set  $D_f=S$ , where  $S=\{(x,y,z):x^2-y^2+z^2\leq 1 \text{ and } x,y,z\geq 0\}$ 

# Which statement is true?

- (a) S is closed and bounded, and f has a maximum value on S
- (b) S is closed and not bounded, and f has a maximum value on S
- (c) S is closed and not bounded, and f does not have a maximum value on S
- (d) S is not closed, and f does not have a maximum value on S
- (e) I prefer not to answer.